

<b>TAFE ID</b>	329428800	<b>Result Slip No</b>	S2519777
<b>Student Name</b>	Rachel Loveday	<b>Date marked</b>	19/10/2021

## Student Feedback Mathematics Assignment 6492MD 3

<b>Result</b>	$\frac{12}{45} = 27\%$
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	Max mark	mark	Teacher's Comments				
Q1 to 3							
1	1	0	B (Note: option B appears twice.)				
2	1	1	B				
3	1	0	D				
			<div>1     If <math>f(x) = (x - 1)^2</math> and <math>g(x) = x</math> , then an expression for <math>\frac{f(x)}{g(x)}</math> is</div> <table><tr><td>A     <math>x - 2 - \frac{1}{x}</math></td><td>B     <math>x - 2 + \frac{1}{x}</math></td></tr><tr><td>BC   <math>x - 1 - \frac{1}{x}</math></td><td>D     <math>x - 1 + \frac{1}{x}</math></td></tr></table> <div><p>Q1) A <del>X</del></p><p>Q2) B ✓</p><p>Q3) A <del>X</del></p></div> <div>1: If <math>f(x) = (x - 1)^2</math> and <math>g(x) = x</math>,</div> <div><math display="block">\frac{f(x)}{g(x)} = \frac{(x - 1)^2}{x} = \frac{x^2 - 2x + 1}{x} = x - 2 + \frac{1}{x}</math></div> <div>3: Differentiate <math>x</math> twice in terms of time to find the acceleration:</div> <div><math display="block">x = 2 t^2 - 3t + 1</math></div> <div>Differentiate <math>x</math> to find the velocity:</div>	A $x - 2 - \frac{1}{x}$	B $x - 2 + \frac{1}{x}$	BC $x - 1 - \frac{1}{x}$	D $x - 1 + \frac{1}{x}$
A $x - 2 - \frac{1}{x}$	B $x - 2 + \frac{1}{x}$						
BC $x - 1 - \frac{1}{x}$	D $x - 1 + \frac{1}{x}$						

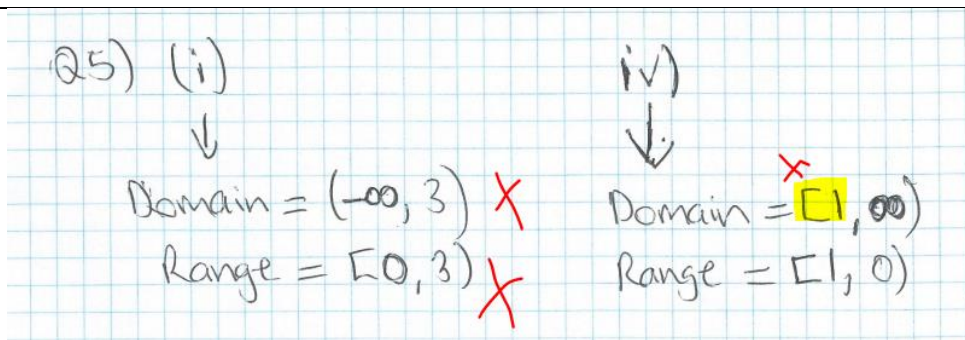
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			$\frac{dx}{dt} = v = 4t - 3$ Differentiate again to find the acceleration: $\frac{dv}{dt} = a = 4 \frac{m}{s^2}$
<b>total</b>	<b>3</b>	<b>1</b>	
<b>Q4</b>			
a	2	1	-0.5/error
			<p>           (Q4)            i) Neither <del>X</del>            ii) Even ✓            iii) Neither ✓            iv) Odd <del>X</del>            v) Neither ✓            vi) Odd ✓            vii) Odd ✓         </p> <p> <i>Note that question a should say relations, not functions as the circle is not a function.</i>   <b>EVEN</b> relations are <b>symmetrical about the y-axis</b> or <math>f(-x) = f(x)</math> for the whole domain.   <b>ODD</b> relations are <b>symmetrical about the origin</b> or <math>f(-x) = -f(x)</math>.         </p>

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			<p>Even relations are i ii. Odd relations are vi vii. Neither are iii iv v.</p>
b	3	0	-0.5/error

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	Max mark	mark	Teacher's Comments
			i $y =  x  + 3$ ii $y = 3 - x^2$ iii $(x - 3)^2 + (y - 3)^2 = 9$ iv $y = 3^x$ v $y =  x + 3 $ vi $y = -3x^3$ vii $y = \frac{3}{x}$
Q4 total	5	1	
Q5			
	2	0	-0.5/error
			 <p>Q5) (i) <math>y =  x  + 3</math>  <math>\downarrow</math>            Domain = <math>(-\infty, 3)</math> <math>\times</math>            Range = <math>[0, 3)</math> <math>\times</math></p> <p>iv) <math>y = 3^x</math>  <math>\downarrow</math>            Domain = <math>[1, \infty)</math> <math>\times</math>            Range = <math>[1, 0)</math> <math>\times</math></p> <p>i <math>y =  x  + 3</math>            domain: <math>x \in \mathbb{R}</math> or <math>(-\infty, \infty)</math> range: <math>y \in \mathbb{R}: y \geq 3</math> or <math>[3, \infty)</math>            ii <math>y = 3^x</math>            domain: <math>x \in \mathbb{R}</math> or <math>(-\infty, \infty)</math> range: <math>y \in \mathbb{R}: y &gt; 0</math> or <math>(0, \infty)</math></p>
Q5 total	2	0	
Q6			
a	3	2	1 each

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	Max mark	mark	Teacher's Comments																																																								
			<div>Q6)</div> <div><div>(2)</div><div>i) <math>f(x) = -x + 2</math> <math>f(-x)</math> <math>= -x(-x + 2)</math> <math>y = x + 2</math> ✓</div><div>ii) <math>f(x) = -x + 2</math> <math>-f(x)</math> <math>= -(-x + 2)</math> <math>y = x - 2</math> ✓</div><div>iii) <math>-f(-x)</math> <math>f(x) = -x + 2</math> <math>-f(-x) = -f(-x)</math> <math>= f(x)</math> <math>= x + 2</math> <math>y = 2x</math> ✗</div></div> <div>iii <math>-f(-x) = -(-(-x) + 2) = -x - 2</math></div> <div>Q6) (b) (i), (ii), (iii), (iv)</div> <table><tr><td>x</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>y</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>x</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>y</td><td>-4</td><td>-3</td><td>-2</td><td>-1</td><td>0</td><td>1</td></tr><tr><td>x</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>y</td><td>-4</td><td>-2</td><td>0</td><td>2</td><td>4</td><td>6</td></tr><tr><td>x</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>y</td><td>4</td><td>3</td><td>2</td><td>1</td><td>0</td><td>-1</td></tr></table> <div></div>	x	-2	-1	0	1	2	3	y	0	1	2	3	4	5	x	-2	-1	0	1	2	3	y	-4	-3	-2	-1	0	1	x	-2	-1	0	1	2	3	y	-4	-2	0	2	4	6	x	-2	-1	0	1	2	3	y	4	3	2	1	0	-1
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	Max mark	mark	Teacher's Comments
			<div> <div>● <math>f(x) = -x + 2</math></div> <hr/> <div>● <math>g(x) = f(-x)</math> → <math>-(-x) + 2</math></div> <hr/> <div>● <math>h(x) = -f(x)</math> → <math>-(-x + 2)</math></div> <hr/> <div>● <math>p(x) = -f(-x)</math> → <math>-(-(-x) + 2)</math></div> </div>
<b>Q6 total</b>	7	5	
<b>Q7</b>			
a	1	1	Correct answer Substitute 5 in t: $\frac{5}{5-1} = \frac{5}{4} = 1\frac{1}{4}$
b	1	1	Correct answer Substitute $x + 1$ into t: $\frac{x+1}{(x+1)-1} = \frac{x+1}{x}$ is correct or you may simplify and get $\frac{x+1}{x} = \frac{x}{x} + \frac{1}{x} = 1 + \frac{1}{x}$
c	1	0	Correct answer



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			$\frac{t}{t-1} = 2$ $t = 2(t-1)$ $t = 2t - 2$ $t = 2$
d	1	0	Correct domain $t \neq 1$ (The denominator cannot equal to zero since dividing by zero is not defined.)
e	1	0	Correct range $g \neq 1$ The range is all real g values except for 1.
f	1	0	Correct asymptotes ( $-0.5/\text{error}$ ) The asymptotes are: $t = 1$ and $g = 1$
			<p>Q7)</p> <p>a) <math>g(t) = \frac{t}{t-1}</math></p> <p><math>g(5) = \frac{5}{5-1}</math></p> <p><math>g(5) = \frac{5}{4}</math> ✓</p> <p>b) <math>g(t) = \frac{t}{t-1}</math></p> <p><math>g(x+1) = \frac{x+1}{(x+1)-1}</math> ✓ = <math>\frac{x+1}{x}</math></p> <p>c) <math>g(t) = \frac{t}{t-1}</math></p> <p><math>g(2) = \frac{2}{2-1}</math></p> <p><math>g(2) = \frac{2}{1}</math></p> <p>= 1</p> <p><del>Q7)</del></p> <p>d) <math>(-\infty, 1)</math></p> <p>e) <math>[5, \infty)</math></p> <p>f) <math>x=2</math> <math>y=1</math></p>
<b>Q7 total</b>	<b>6</b>	<b>2</b>	

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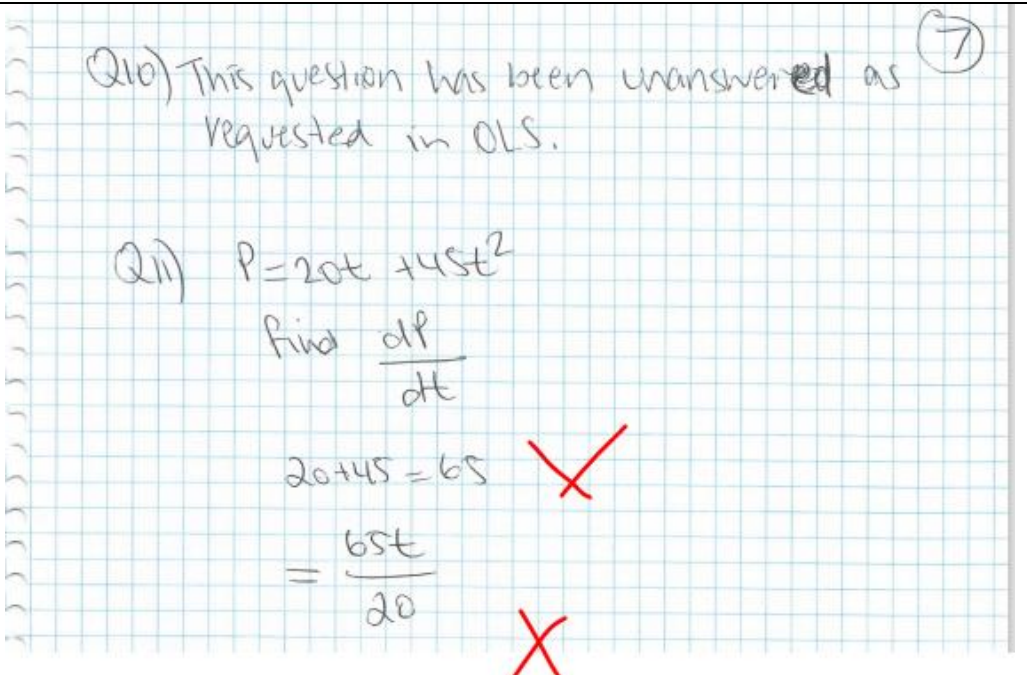
	Max mark	mark	Teacher's Comments
<b>Q8</b>			
a	2	0	1 for correct completing of squares, 1 for rearranging
b	2	1	Correct coordinates for centre and correct radius (1 each)
			<p>Q8)</p> <p>a) <math>x^2 + y^2 + 2x - 4y - 44 = 0</math></p> <p><math>x^2 + y^2 + 2x - 4y = 44</math></p> <p><math>x^2 + y^2 + x - 4y = 44 + 1</math> <math>\left(\frac{2}{2}\right)^2 = 1^2 = 1</math></p> <p><math>x^2 + y^2 + x - y = 45 + 4</math> <math>\left(\frac{4}{2}\right)^2 = 2^2 = 4</math></p> <p><math>\rightarrow (x^2 + y^2) + (x - y) = 49</math></p> <p><math>(x - x_0)^2 + (y - y_0)^2 = 49 \text{ (r}^2\text{)}</math></p> <p><math>r^2 = 49</math> ✓</p> <p>b) Radius <del>is</del></p> <p>↓</p> <p><math>r^2 = 49</math></p> <p><math>r = \sqrt{49}</math></p> <p><math>r = 7 \text{ units}</math> ✓</p> <p>Centre = 3.5 units ✗</p> <p><math>(x + 1)^2 - 1 + (y - 2)^2 - 4 - 44 = 0</math></p> <p><math>(x + 1)^2 + (y - 2)^2 = 49</math></p> <p>Centre is <math>(-1, 2)</math> and radius <math>r = 7</math></p>
<b>Q8 total</b>	4	1	
<b>Q9</b>			
a	2	0	Correct coordinates for P and Q $(-0.5/\text{error})$
b	2	0	Correct gradient of PQ
c	1	0	Correct limit of gradient



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	Max mark	mark	Teacher's Comments
			<p>Q9)</p> <p>a) <math>y = 2x^2 - 5</math>  <math>y = 2 \times 2^2 - 5</math>  <math>y = (2 \times 4) - 5</math>  <math>y = 8 - 5</math>  <math>y = 3</math>  <math>P = (2, 3)</math>  <math>y = 2x^2 - 5</math>  <math>y = 2 \times 3^2 - 5</math>  <math>y = (2 \times 9) - 5</math>  <math>y = 18 - 5</math>  <math>y = 13</math>  <math>Q = (3, 13)</math></p> <p>b) <math>m = \frac{y^2 - y^1}{x^2 - x^1}</math>  <math>m = \frac{13 - 3}{3 - 2}</math>  <math>m = \frac{10}{1}</math>  <math>m = 10</math></p> <p>c) <math>Q = x + h</math>  <math>Q = 3 + 13 = 16</math>  <math>h \rightarrow 0</math>  <math>\frac{dy}{dx} = \frac{13}{3}</math>  <math>= 4.33</math></p> <p>This topic is explained in Differentiation from first principles.</p> <p>a:  <math>P(x, 2x^2 - 5)</math> , <math>Q(x+h, 2(x+h)^2 - 5)</math></p> <p>b:  <math>m_{PQ} = \frac{2(x+h)^2 - 5 - (2x^2 - 5)}{x+h-x}</math>  <math>= \frac{2(x^2 + 2xh + h^2) - 5 - 2x^2 + 5}{h}</math>  <math>= \frac{4xh + 2h^2}{h}</math>  <math>= \frac{2h(2x + h)}{h}</math>  <math>= 2(2x + h)</math></p> <p>c:  <math>\lim_{h \rightarrow 0} [2(2x + h)] = 2(2x)</math>  <math>= 4x</math></p>
<b>Q9 total</b>	5	0	

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	Max mark	mark	Teacher's Comments
<b>Q10 deleted question</b>			
	2		Factorises the expression $\frac{3x-3}{x^2-1}$ and obtains correct limit
	2		Divides both numerator and denominator with $x^2$ , and obtains correct limit
			$LHS = \lim_{x \rightarrow 1} \frac{3(x-1)}{(x-1)(x+1)}$ $= \lim_{x \rightarrow 1} \left( \frac{3}{x+1} \right)$ $= \frac{3}{2}$ $= 1\frac{1}{2}$
<b>Q10 total</b>	<b>4</b>		deleted
<b>Q11</b>			
	2	0	Correct differentiation of P with respect to r
			 <p>Q10) This question has been unanswered as requested in OLS. (7)</p> <p>Q11) <math>P = 20t + 45t^2</math>  Find <math>\frac{dP}{dt}</math>  <math>20 + 45 = 65</math> ✓  <math>= \frac{65t}{20}</math> ✓</p>

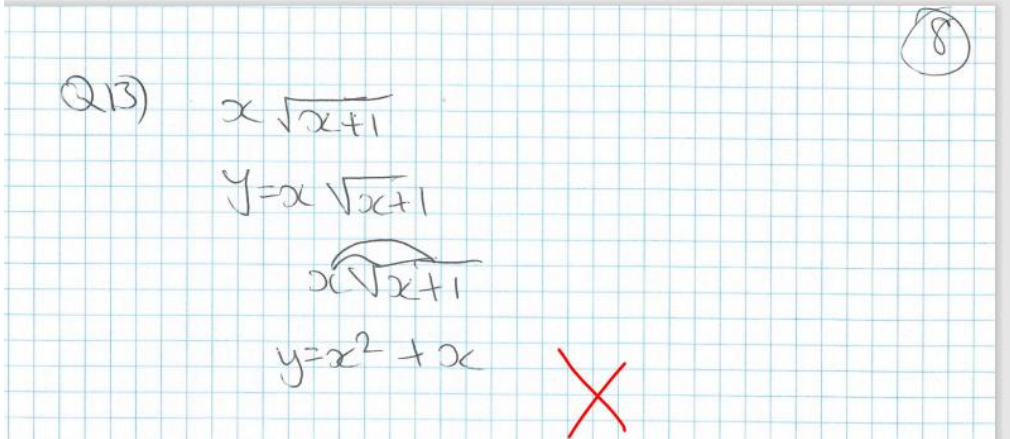
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			<p><b>436</b> <b>MATHS IN FOCUS 11.</b> Mathematics Extension 1 <span style="float: right;">ISBN 9780170413299</span></p> <p><b>EXAMPLE 10</b></p> <p><b>h</b> Differentiate <math>S = 6r^2 - 12r</math> with respect to <math>r</math>.</p> <p><b>h</b> Differentiating with respect to <math>r</math> rather than <math>x</math>:</p> $S = 6r^2 - 12r$ $\frac{dS}{dr} = 12r - 12$ <p>As in the textbook example above, differentiate P with respect to t:</p> $\frac{dP}{dt} = 20 + 90t$
<b>Q11 total</b>	2	0	
<b>Q12</b>			
	1	0	Rewrites y in index form
	2	0	Correct differentiation

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			<p>Q12) <math>1.5\sqrt{x^3} - \frac{4}{x}</math></p> <p><math>f(x) = 1.5\sqrt{x^3} = 1.5x^{\frac{3}{2}}</math> <span style="color: red; font-size: 2em;">X</span></p> <p><math>= 1.5 \times \frac{1}{2} x^{\frac{3}{2}-1}</math></p> <p><math>= \frac{1.5}{2} x^{\frac{1}{2}}</math></p> <p><math>= \frac{1.5}{2} \times \frac{1}{x^{-\frac{1}{2}}}</math></p> <p><math>= \frac{1.5}{2} \times \frac{1}{\sqrt{x}}</math></p> <p><math>= \frac{1.5}{2\sqrt{x}}</math> <span style="color: red; font-size: 2em;">X</span></p> <p>First, write both terms in the expression in index form, then apply the index rule of differentiation.</p> <p>In the textbook, these two topics cover what you need to know. Short methods of differentiation and Derivatives and indices.</p> $\frac{d}{dx} \left( 1.5\sqrt{x^3} - \frac{4}{x} \right) = \frac{d}{dx} \left( 1.5x^{\frac{3}{2}} - 4x^{-1} \right)$ $= 2.25x^{\frac{1}{2}} + 4x^{-2}$ $= 2.25\sqrt{x} + \frac{4}{x^2}$
<b>Q12 total</b>	3	0	
<b>Q13</b>			
	2	0	Correct $u'$ and $v'$

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	Max mark	mark	Teacher's Comments
	2	0	Correct product rule
			 <p>Rachel, you needed to apply the product rule <math>(u \times v)' = u'v + uv'</math>, where:</p> $x = u \quad \text{and} \quad v = \sqrt{x+1}$ $x' = 1 \quad \quad \quad v' = \frac{1}{2\sqrt{x+1}}$ $\frac{d}{dx} x\sqrt{x+1} = \frac{d}{dx} x(x+1)^{\frac{1}{2}}$ $= x \cdot \frac{1}{2}(x+1)^{-\frac{1}{2}} + (x+1)^{\frac{1}{2}} \cdot 1$ $= \frac{x}{2\sqrt{x+1}} + \frac{\sqrt{x+1}}{1}$ $= \frac{x+2(x+1)}{2\sqrt{x+1}}$ $= \frac{3x+2}{2\sqrt{x+1}}$
<b>Q13 total</b>	4	0	
<b>Q14</b>			
	1	0	Correct $u'$ and $v'$
	3	2	Correct quotient rule



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			<p>Q14) <math>\frac{x^2+3}{2x+7}</math></p> <p><math>y = \frac{u}{v}</math> where <math>u = x^2+3</math> ✓  <math>v = 2x+7</math> ✓  <math>u' = 3</math> ✗ <math>2x</math>  <math>v' = 7</math> ✗ <math>2</math></p> <p><math display="block">= \frac{3(x^2+3) - 7(2x+7)}{(2x+7)^2}</math></p> <p><math display="block">= \frac{3x^2+9-14x-49}{(2x+7)^2}</math></p> <p><math display="block">= \frac{3x^2-14x-40}{(2x+7)^2}</math></p> <p>Apply the quotient rule:</p> $\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2}$ $\frac{d}{dx} \left( \frac{x^2+3}{2x+7} \right) = \frac{(2x+7) \cdot 2x - (x^2+3) \cdot 2}{(2x+7)^2}$ $= \frac{4x^2+14x-2x^2-6}{(2x+7)^2}$ $= \frac{2x^2+14x-6}{(2x+7)^2}$
<b>Q14 total</b>	4	2	

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### Teacher's Comment

Rachel,

The assignment was based on Further Functions and Introduction to Calculus Chapters. Calculus is a foundation for the all the calculus-based topics.

Regards,

Anna Fazekas  
Maths Teacher